

## 3-2 Study Guide and Intervention

### Solving Linear Equations by Graphing

**Solve by Graphing** You can solve an equation by graphing the related function. The solution of the equation is the  $x$ -intercept of the function.

**Example:** Solve the equation  $2x - 2 = -4$  by graphing.

First set the equation equal to 0. Then replace 0 with  $f(x)$ . Make a table of ordered pair solutions. Graph the function and locate the  $x$ -intercept.

$$2x - 2 = -4$$

Original equation

$$2x - 2 + 4 = -4 + 4$$

Add 4 to each side.

$$2x + 2 = 0$$

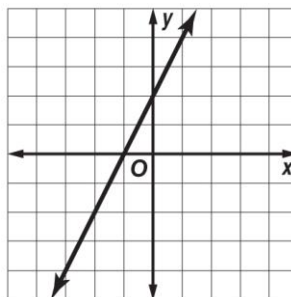
Simplify.

$$f(x) = 2x + 2$$

Replace 0 with  $f(x)$ .

To graph the function, make a table. Graph the ordered pairs.

$x$	$f(x) = 2x + 2$	$f(x)$	$[x, f(x)]$
1	$f(1) = 2(1) + 2$	4	(1, 4)
-1	$f(-1) = 2(-1) + 2$	0	(-1, 0)
-2	$f(-2) = 2(-2) + 2$	-2	(-2, -2)



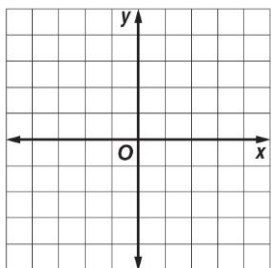
The graph intersects the  $x$ -axis at  $(-1, 0)$ .

The solution to the equation is  $x = -1$ .

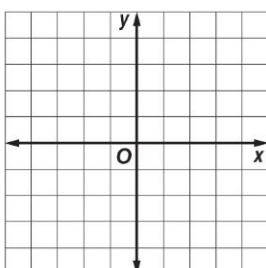
### Exercises

**Solve each equation by graphing.**

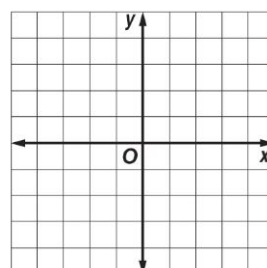
1.  $3x - 3 = 0$



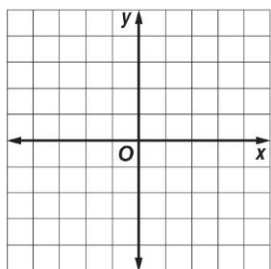
2.  $-2x + 1 = 5 - 2x$



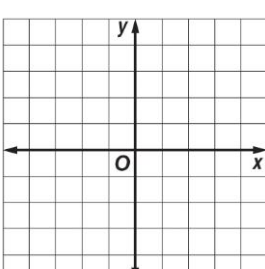
3.  $-x + 4 = 0$



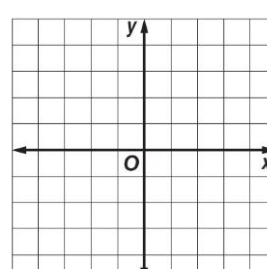
4.  $0 = 4x - 1$



5.  $5x - 1 = 5x$



6.  $-3x + 1 = 0$



## 3-2 Study Guide and Intervention (continued)

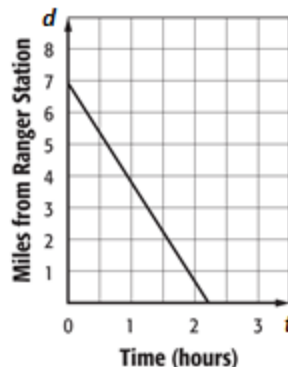
### Solving Linear Equations by Graphing

**Estimate Solutions by Graphing** Sometimes graphing does not provide an exact solution, but only an estimate. In these cases, solve algebraically to find the exact solution.

**Example: WALKING** You and your cousin decide to walk the 7-mile trail at the state park to the ranger station. The function  $d = 7 - 3.2t$  represents your distance  $d$  from the ranger station after  $t$  hours. Find the zero of this function. Describe what this value means in this context.

Make a table of values to graph the function.

$t$	$d = 7 - 3.2t$	$d$	$(t, d)$
0	$d = 7 - 3.2(0)$	7	$(0, 7)$
1	$d = 7 - 3.2(1)$	3.8	$(1, 3.8)$
2	$d = 7 - 3.2(2)$	0.6	$(2, 0.6)$

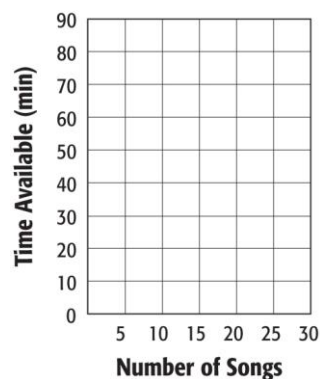


The graph intersects the  $t$ -axis between  $t = 2$  and  $t = 3$ , but closer to  $t = 2$ . It will take you and your cousin just over two hours to reach the ranger station.

You can check your estimate by solving the equation algebraically.

### Exercises

- 1. MUSIC** Jessica wants to record her favorite songs to one CD. The function  $C = 80 - 3.22n$  represents the recording time  $C$  available after  $n$  songs are recorded. Find the zero of this function. Describe what this value means in this context.



- 2. GIFT CARDS** Enrique uses a gift card to buy coffee at a coffee shop. The initial value of the gift card is \$20. The function  $n = 20 - 2.75c$  represents the amount of money still left on the gift card  $n$  after purchasing  $c$  cups of coffee. Find the zero of this function. Describe what this value means in this context.

