

had her hair cut to a length of 10 inches. If her hair grows at a rate of 0.02 inch per day, which equation represents the length (L) of Theresa's hair, in inches, after d days?

$$L = 0.2 + 10d$$

$$L = 10 + 0.2d$$

$$L = 0.2 + 10d$$

$$L = 10 + 0.2d$$

Which set contains only ordered pairs that satisfy $y = 3x + 7$?

(2, 13) and (4, 18)

(3, 16) and (5, 22)

(4, 19) and (6, 24)

(5, 22) and (7, 27)

Ms. Hernandez wrote four sets of ordered pairs on the whiteboard for her math students.

Which set is y a function of x ?

{(3, -2), (3, -2), (-2, 1), (2, 1), (0, 0)}

{(1, -2), (4, 2), (2, -4), (2, 4), (4, 4)}

{(1, 2), (4, 3), (-1, 5), (-6, -2), (-2, 1)}

{(1, 2), (4, 5), (-3, -3), (0, -1), (6, -2)}

Example 1 Factor Differences of Squares

Factor each polynomial.

a. $16h^2 - 9a^2$

$$16h^2 - 9a^2 = (4h)^2 - (3a)^2$$

$$= (4h + 3a)(4h - 3a)$$

Write in the form of $a^2 - b^2$

Factor the difference of squares.

(A) $(4h)^2 - (3a)^2$

b. $121 - 4b^2$

$$121 - 4b^2 = (11)^2 - (2b)^2$$

$$= (11 - 2b)(11 + 2b)$$

Write in the form of $a^2 - b^2$

Factor the difference of squares

$(4h+3a)(4h-3a)$

c. $27g^3 - 3g$

Because the terms have a common factor, factor out the GCF first.
Then proceed with other factoring techniques.

$$27g^3 - 3g = 3g(9g^2 - 1)$$

$$= 3g[(3g)^2 - (1)^2]$$

$$= 3g(3g - 1)(3g + 1)$$

Factor out the GCF of $3g$.

Write in the form $a^2 - b^2$

Factor the difference of squares

$16h^2 - 9a^2$
 $16h^2 - 12ah + 12ah - 9a^2$
 $(4h+3a)(4h-3a)$

Guided Practice

1A. $81 - c^2$

1C. $9x^3 - 4x$

1B. $64g^2 - h^2$

1D. $-4y^3 + 9y$

(C) $3g(9g^2 - 1)$
 $3g[(3g)^2 - (1)^2]$
 $3g[(3g+1)(3g-1)]$

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$$\begin{aligned} \textcircled{a} \quad & 81 - c^2 \\ & (9)^2 - (c)^2 \\ & (9+c)(9-c) \end{aligned}$$

$$\begin{aligned} \textcircled{b} \quad & 64g^2 - h^2 \\ & (8g)^2 - (h)^2 \\ & (8g+h)(8g-h) \end{aligned}$$

$$\begin{aligned}
 \textcircled{c} \quad & 9x^3 - 4x \\
 & x(9x^2 - 4) \\
 & x[(3x)^2 - (2)^2] \\
 & x[(3x+2)(3x-2)]
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{d} \quad & -4y^3 + 9y \\
 & -y(4y^2 - 9) \\
 & -y[(2y)^2 - (3)^2] \\
 & -y[(2y+3)(2y-3)]
 \end{aligned}$$

Example 2 Apply a Technique More than Once

Factor each polynomial.

a. $b^4 - 16$

$$\begin{aligned}b^4 - 16 &= (b^2)^2 - (4)^2 \\&= (b^2 + 4)(b^2 - 4) \\&= (b^2 + 4)(b^2 - 2^2) \\&= (b^2 + 4)(b + 2)(b - 2)\end{aligned}$$

Write $b^4 - 16$ in $a^2 - b^2$ form.

Factor the difference of squares.

 $b^2 - 4$ is also a difference of squares.

Factor the difference of squares.

b. $625 - x^4$

$$\begin{aligned}625 - x^4 &= (25)^2 - (x^2)^2 \\&= (25 + x^2)(25 - x^2) \\&= (25 + x^2)(5^2 - x^2) \\&= (25 + x^2)(5 - x)(5 + x)\end{aligned}$$

Write $625 - x^4$ in $a^2 - b^2$ form.

Factor the difference of squares.

Write $25 - x^2$ in $a^2 - b^2$ form.

Factor the difference of squares.

Guided Practice

2A. $y^4 - 1$

2C. $81 - x^4$

2B. $4a^4 - b^4$

2D. $16y^4 - 1$

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Example 1 Recognize and Factor Perfect Square Trinomials

Determine whether each trinomial is a perfect square trinomial. Write *yes* or *no*.
If so, factor it.

a. $4y^2 + 12y + 9$

- 1 Is the first term a perfect square? Yes, $4y^2 = (2y)^2$.
- 2 Is the last term a perfect square? Yes, $9 = 3^2$.
- 3 Is the middle term equal to $2(2y)(3)$? Yes, $12y = 2(2y)(3)$

Since all three conditions are satisfied, $4y^2 + 12y + 9$ is a perfect square trinomial.

$$4y^2 + 12y + 9 = (2y)^2 + 2(2y)(3) + 3^2 \\ = (2y + 3)^2$$

Write as $a^2 + 2ab + b^2$
Factor using the pattern.

b. $9x^2 - 6x + 4$

- 1 Is the first term a perfect square? Yes, $9x^2 = (3x)^2$.
- 2 Is the last term a perfect square? Yes, $4 = 2^2$.
- 3 Is the middle term equal to $-2(3x)(2)$? No, $-6x \neq -2(3x)(2)$.

Since the middle term does not satisfy the required condition, $9x^2 - 6x + 4$ is not a perfect square trinomial.

Guided Practice

1A. $9y^2 + 24y + 16$

1B. $2a^2 + 10a + 25$

Handwritten work for Example 1a:

$$4y^2 + 12y + 9$$

Diagram showing the perfect square trinomial structure:

$$\begin{array}{ccc} (2y)^2 & & (3)^2 \\ & \searrow & \nearrow \\ & 12y & \end{array}$$

Diagram showing the perfect square trinomial structure for 1B:

$$\begin{array}{ccc} (3x)^2 & & (2)^2 \\ & \searrow & \nearrow \\ & 12x & \end{array}$$

Handwritten notes:

- For 1A, $(2y)^2$ and $(3)^2$ are written, with a checkmark next to $12y$.
- For 1B, $(3x)^2$ and $(2)^2$ are written, with a checkmark next to $12x$.
- The expression $2y + 3$ is circled in red.

$$\textcircled{A} \quad 9y^2 + 24y + 16$$

$$\begin{array}{cc} (3y) & (4) \\ & \swarrow \searrow \\ & (12y) \end{array}$$

$$\begin{array}{c} 2 \\ 24y \end{array}$$

yes

$$(3y+4)^2$$

$$\textcircled{B} \quad 2a^2 + 10a + 25$$

$$2a^2 = 10$$

Practice

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